



Field Evidence Model: A hierarchical heterogeneous structure for subsurface transport modelling

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Introduction & Objective

- prediction of solute behavior in groundwater valuable for risk assessment, remediation etc.
- solute mass distribution strongly influenced by unknown aquifer heterogeneity
- lack of data for parametrization and calibration
- novel hierarchical conductivity structure combining deterministic information and simple statistics
- incorporating aquifer features of different scales following field evidence
- implementation for MADE & sensitivity analysis

Approach: Concept & Scales

- modules capturing features of heterogeneity according to scales (large, intermediate, local)
- deterministic/stochastic representation depending on ergodic conditions
- structural parameters from characteristic investigation methods



Relevant scales: M - domain scale L - plume scale D - Detection scale (device specific)

I - Heterogeneity scales: • Large scale: $I_1 \sim M > L$ • Intermediate: $I_2 \sim L > M$

• Local: I₃ > L >> M

Approach: Conductivity Modules

A) Large Scale Structures

- character: regional trends, facies
- concept: deterministic zones
- observations: piezometric surface map, pumping tests

B) Intermediate Scale Heterogeneity

- character: preferential flow paths, stagnant areas
- concept: binary inclusion distribution (discrete, stochastic)
- observations: few borehole logs, e.g. flowmeter, DPIL

C) Small Scale Heterogeneity

- character: local fluctuations
- concept: log-normal spatial variable (continuous random)
- observations: geostatistics, e.g. flowmeter, DPIL







Gaussian field with fluctuations: Concept exponential covariance. Left: $\lambda_1 = 2$, $\lambda_y = 1$ (e=0.5); Right: $\lambda_1 = 5$, $\lambda_y = 0.5$ (e=0.1).

Results: Mass Distribution



Longitudinal mass distributions M(x) for conductivity concepts (A = yellow), (A+B = blue), (A+B+C = green) of MADE aquifer versus tracer experiment observations (red): for 6 times (panels) in linear scale with subplot in log-scale. Data is aggregated over intervals of 10m distance as established for MADE experiment data.

Results: Impact of Parameters



(A+B) for standard setting (black) and various input parameters (colors): inclusion length I_{I} , amount of inclusion p, distance of zone interface x, to injection and mean conductivity K_1 of zone 1 (source area). MADE experiment in red.



Cumulative mass distributions: A = yellow, A+B = blue, A+B+C = green, MADE experiment = red.

Observation locations

at MADE site



Breakthrough curves M(t) for structures (A) and (A+B) at distances x from the injection.

Example: Transport at MADE

A) Deterministic Zones

B) Heterogeneous Inclusions

C) Small Scale Heterogeneity





Conclusions

References

The MADE Site (Columbus, Mississippi)

• field campaigns: *Boggs et al.*, *Rehfeldt et al.* 1992 transport experiment: natural gradient flow with forced pulse injection of bromide

 Iongitudinal mass distribution M(x) for 6 times: T=49,126,202,279,370,503 days after injection

• 2 zones, locations from piezometric surface map • zone's average K-values from pumping tests: K₇₁=2e-6 m/s; K₇₂=2e-4 m/s

• binary distribution with low K₁ & high K₂ value • inclusion's frequency: p =10-20% from flowmeter logs • inclusions lengths: $L_1 = 5-20m$, $L_2 = 0.5-1m$

• flowmeter (*Rehfeldt et al., 1992, Bohling et al., 2016*) • log-K variance: $\sigma_v^2 = 4.5$

• correlation lenghts: $l_{h}=10m$, $l_{v}=1m$

Conceptual Conductivity Structures:

(A) deterministic blocks

(A+B) inclusions in blocks

(A+B+C) inclusions in blocks and random fluctuations

• goal-oriented site specific transport analysis: (i) Model parametrisation adapted to available measurements at field site

(ii) Representation of critical features of heterogeneity (iii) Focus on minimal characterization requirements • simple conductivity structures able to reproduce skewed mass plumes

 combining deterministic and stochastic approaches reduces required observation data

 binary structure is alternative to Gaussian distribution which needs geostatistical analysis

1 - Boggs, Young, Beard, Gelhar, Rehfeldt & Adams, 1992; Field study of dispersion in a heterogeneous aquifer: 1. Overview and site description; WRR 28; doi: 10.1029/92WR01756

2 - Rehfeldt, Boggs & Gelhar, 1992; Field Study of Dispersion in a Heterogeneous Aquifer: 3. Geostatistical Analysis of Hydraulic Conductivity; WRR 28; 10.1029/92WR01758

3 - Bohling, Liu, Dietrich & Butler, 2016; Reassessing the MADE direct-push hydraulic conductivity data using a revised calibration procedure; WRR 52; doi: 10.1002/2016WR019008